

Solving trig equations with double angles		
1	Solve the equation $\cos 2x + 5\cos x - 2 = 0$	for $0 \leq x \leq 360^\circ$. 5
2	Solve the equation $\sin 2x - \cos x = 0$	for $0 \leq x \leq 180^\circ$. 4
3	Solve the equation $3\cos 2x + \cos x = -1$	for $0 \leq x \leq 360^\circ$. 5
4	Solve the equation $5\sin x - 4 = 2\cos 2x$	for $0 \leq x \leq 2\pi$. 5
5	Solve the equation $\cos 2x + 2\sin x = \sin^2 x$	for $0 \leq x \leq 360^\circ$. 5
6	Solve the equation $\sin x - 2\cos 2x = 1$	for $0 \leq x \leq 2\pi$. 5

Double Angle Equations – Answers	
1	<p>Replace $\cos 2x$ with $2\cos^2 x - 1$ $2\cos^2 x - 1 + 5\cos x - 2 = 0$</p> <p>Simplify and equate to zero $2\cos^2 x + 5\cos x - 3 = 0$</p> <p>Factorise $(2\cos x - 1)(\cos x + 3) = 0$</p> <p>Solve for each factor $(2\cos x - 1) = 0, \cos x = \frac{1}{2}, x = 60^\circ$ and 300° $(\cos x + 3) = 0, \cos x = -3, \text{ no solutions}$</p>
2	<p>Replace $\sin 2x$ with $2\sin x \cos x$ $2\sin x \cos x - \cos x = 0$</p> <p>Factorise $\cos x(2\sin x - 1) = 0$</p> <p>Solve for each factor $\cos x = 0, x = 0^\circ$ and 360° $(2\sin x - 1) = 0 \Rightarrow \sin x = \frac{1}{2}, x = 30^\circ$ and 150°</p>
3	<p>Replace $\cos 2x$ with $2\cos^2 x - 1$ $3(2\cos^2 x - 1) + \cos x = -1$</p> <p>Simplify and equate to zero $6\cos^2 x + \cos x - 2 = 0$</p> <p>Factorise $(2\cos x - 1)(3\cos x + 2) = 0$</p> <p>Solve for each factor $(2\cos x - 1) = 0, \cos x = \frac{1}{2}, x = 60^\circ$ and 300° $(3\cos x + 2) = 0, \cos x = -\frac{2}{3}, x = 138^\circ$ and 228°</p>
4	<p>Replace $\cos 2x$ with $1 - 2\sin^2 x$ $5\sin x - 4 = 2(1 - 2\sin^2 x)$</p> <p>Simplify and equate to zero $5\sin x - 4 = 2 - 4\sin^2 x$ $4\sin^2 x + 5\sin x - 6 = 0$</p> <p>Factorise $(4\sin x - 3)(\sin x + 2) = 0$</p> <p>Solve for each factor $(4\sin x - 3) = 0, \sin x = \frac{3}{4}, x = 0.848, 2.29$ $(\sin x + 2) = 0, \sin x = -2, \text{ no solutions}$</p> <p>Make sure that your final answers are in radians</p>
5	<p>Replace $\cos 2x$ with $1 - 2\sin^2 x$ $1 - 2\sin^2 x + 2\sin x = \sin^2 x$</p> <p>Simplify and equate to zero $3\sin^2 x - 2\sin x - 1 = 0$</p> <p>Factorise $(3\sin x + 1)(\sin x - 1) = 0$</p> <p>Solve for each factor $(3\sin x + 1) = 0, \sin x = -\frac{1}{3}, x = 199.5^\circ$ and 340.5° $(\sin x - 1) = 0, \sin x = 1, x = 90^\circ$</p>
6	<p>Replace $\cos 2x$ with $1 - 2\sin^2 x$ $\sin x - 2(1 - 2\sin^2 x) = 1$</p> <p>Simplify and equate to zero $4\sin^2 x + \sin x - 3 = 0$</p> <p>Factorise $(4\sin x - 3)(\sin x + 1) = 0$</p> <p>Solve for each factor $(4\sin x - 3) = 0, \sin x = \frac{3}{4}, x = 0.848, 2.29$ $(\sin x + 1) = 0, \sin x = -1, x = \frac{3\pi}{2}$</p> <p>Make sure that your final answers are in radians</p>