

Polynomials		
1	<p>(a) Show that $(x - 1)$ is a factor of $2x^3 + x^2 - 8x + 5$</p> <p>(b) Hence fully factorise $2x^3 + x^2 - 8x + 5$</p> <p>(c) Solve $2x^3 + x^2 - 8x + 5 = 0$</p>	<p>2</p> <p>3</p> <p>1</p>
2	<p>(a) Show that $(x - 4)$ is a factor of $x^3 - 5x^2 + 2x + 8$</p> <p>(b) Hence fully factorise $x^3 - 5x^2 + 2x + 8$</p> <p>(c) Solve $x^3 - 5x^2 + 2x + 8 = 0$</p>	<p>2</p> <p>3</p> <p>1</p>
3	<p>(a) Show that $(x - 1)$ is a factor of $f(x) = 3x^3 + 4x^2 - 5x - 2$ and hence factorise $f(x)$ fully</p> <p>(b) Solve $3x^3 + 4x^2 - 5x - 2 = 0$</p>	<p>5</p> <p>1</p>
4	Fully factorise $2x^3 + 5x^2 - 4x - 3$	5
5	<p>(a) Show that $x = 2$ is a root of the equation $2x^3 + x^2 - 13x + 6 = 0$</p> <p>(b) Hence find the other roots</p>	<p>5</p> <p>1</p>
6	<p>(a) Show that $(x - 2)$ is a factor of $x^3 - 3x^2 + 4$</p> <p>(b) Hence fully factorise this polynomial</p> <p>(c) Solve $x^3 - 3x^2 + 4 = 0$</p> <p>(d) Identify the coordinates of the turning point at the x-axis</p>	<p>2</p> <p>3</p> <p>1</p> <p>1</p>

Polynomials - Answers	
1.	<p>using synthetic division for $x = 1$</p> $\begin{array}{r rrrr} 1 & 2 & 1 & -8 & 5 \\ & 0 & 2 & 3 & -5 \\ \hline & 2 & 3 & -5 & 0 \end{array}$ <p>No remainder, $(x - 1)$ is a factor $2x^3 + x^2 - 8x + 5 = (x - 1)(2x^2 + 3x - 5)$ $= (x - 1)(2x + 5)(x - 1)$ Solutions are $x = 1, x = -5/2, x = 1$</p>
2.	<p>using synthetic division for $x = 4$</p> $\begin{array}{r rrrr} 4 & 1 & -5 & 2 & 8 \\ & 0 & 4 & -4 & -8 \\ \hline & 1 & -1 & -2 & 0 \end{array}$ <p>No remainder, $(x - 4)$ is a factor $x^3 - 5x^2 + 2x + 8 = (x - 4)(x^2 - x - 2)$ $= (x - 4)(x + 1)(x - 2)$ solutions are $x = 4, x = -1, x = 2$</p>
3	<p>using synthetic division for $x = 1$</p> $\begin{array}{r rrrr} 1 & 3 & 4 & -5 & -2 \\ & 0 & 3 & 7 & 2 \\ \hline & 3 & 7 & 2 & 0 \end{array}$ <p>No remainder, $(x - 1)$ is a factor $3x^3 + 4x^2 - 5x - 2 = (x - 1)(3x^2 + 7x + 2)$ $= (x - 1)(3x + 1)(x + 2)$ solutions are $x = 1, x = -1/3, x = -2$</p>
4	<p>using synthetic division for $x = 1$</p> $\begin{array}{r rrrr} 1 & 2 & 5 & -4 & -3 \\ & 0 & 2 & 7 & 3 \\ \hline & 2 & 7 & 3 & 0 \end{array}$ <p>No remainder, $(x - 1)$ is a factor $2x^3 + 5x^2 - 4x - 3 = (x - 1)(2x^2 + 7x + 3)$ $= (x - 1)(2x + 1)(x + 3)$ Solutions are $x = 1, x = -1/2, x = -3$</p>
5	<p>using synthetic division for $x = 2$</p> $\begin{array}{r rrrr} 2 & 2 & 1 & -13 & 6 \\ & 0 & 4 & 10 & -6 \\ \hline & 2 & 5 & -3 & 0 \end{array}$ <p>No remainder, $(x - 2)$ is a factor, $x = 2$ is a root $2x^3 + x^2 - 13x + 6 = (x - 2)(2x^2 + 5x - 3)$ $= (x - 2)(2x - 1)(x + 3)$ roots are $x = 2, x = 1/2$ and $x = -3$</p>
6	<p>using synthetic division for $x = 2$</p> $\begin{array}{r rrrr} 2 & 1 & -3 & 0 & 4 \\ & 0 & 2 & -2 & -4 \\ \hline & 1 & -1 & -2 & 0 \end{array}$ <p>No remainder, $(x - 2)$ is a factor $x^3 - 3x^2 + 4 = (x - 2)(x^2 - x - 2)$ $= (x - 2)(x - 2)(x + 1)$ Solutions are $x = 2, x = 2$ and $x = -1$ The double root $x = 2$ shows a turning point at $(2,0)$</p>