transformations

[SQA] 1. The diagram shows a sketch of the function y = f(x).

- (*a*) Copy the diagram and on it sketch the graph of y = f(2x).
- (*b*) On a separate diagram sketch the graph of y = 1 f(2x).



C (6, 4)

[SQA] 2. Part of the graph of y = f(x) is shown in the diagram. On separate diagrams sketch the graphs of

- $(a) \quad y=f(x+1)$
- $(b) \quad y=-2f(x).$

Indicate on each graph the images of O, A, B, C and D.



- (*a*) State the values of *a* and *b*.
- (*b*) Sketch the graph of $y = \log_2(x+1) 3$.



A(1,-2)

SQA] 4. (a) Express
$$f(x) = x^2 - 4x + 5$$
 in the form $f(x) = (x - a)^2 + b$. 2

- (*b*) On the same diagram sketch:
 - (i) the graph of y = f(x);
 - (ii) the graph of y = 10 f(x).
- (c) Find the range of values of x for which 10 f(x) is positive.

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[SQA] 5. The sketch shows the graph of y = f(x) for $-2 \le x \le 4$. The function g(x) has the line x = 4 as an axis of symmetry and g(x) = f(x) for $-2 \le x \le 4$.

> On separate sketches indicate (a) y = g(x) for $-2 \le x \le 10$ (b) y = -2g(x) for $0 \le x \le 8$



[SQA] 6. The diagram shows the graph of y = f(x). Sketch the graph of y = 2 - f(x).



(i)
$$y = f(x-1)$$

(ii)
$$y = -f(x) - 2$$

indicating on each graph the images of A, B, C and D.





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[SQA] 8. The diagram shows a sketch of the parabola y = f(x).



(a)	Copy the sketch of $y = f(x)$. On your diagram, draw the parabola with	
	equation $y = -f(x) + 3$.	(4)
(b)	State the values of x for which $3 - f(x) \ge 0$.	(2)
(c)	If $g(x) = 3 - f(x)$, express $g(x)$ in terms of x.	(3)

[SQA] 9. Make a copy of this graph of $y = \log_{10} x$. On your copy, sketch the graph of $y = \log_{10}(x-2)$.



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[SQA] 10. A sketch of the graph of y = f(x) where $f(x) = x^3 - 6x^2 + 9x$ is shown below. The graph has a maximum at A and a minimum at B(3,0).



- (a) Find the coordinates of the turning point at A.
- (*b*) Hence sketch the graph of y = g(x) where g(x) = f(x + 2) + 4. Indicate the coordinates of the turning points. There is no need to calculate the coordinates of the points of intersection with the axes.
- (c) Write down the range of values of k for which g(x) = k has 3 real roots.

[SQA] 11. The diagram shows a sketch of part of the graph of $y = \log_5 x$.

[SQA]



- (b) Make a copy of this diagram and on it sketch the graph of $y = a^{2x}$.
- (c) Find the coordinates of the point of intersection of $y = a^{2x}$ with the line x = 1.



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[END OF QUESTIONS]