

Grade Booster 1

A skier starts from rest and skis straight down a slope inclined at an angle θ to the horizontal, where $\sin \theta = \frac{1}{4}$. The coefficient of friction between the skis and the snow is 0.125.

Find the speed of the skier after she has travelled 75 metres.

4

A bicycle and rider have a total mass of 70 kg. They are travelling at 12 m s^{-1} . The cyclist applies the brakes for 1.5 seconds, resulting in a total resistive force of 180 newtons.

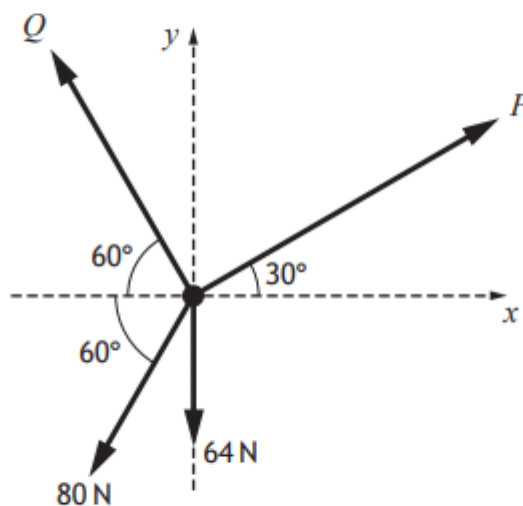
What is the speed of the bicycle after 1.5 seconds?

3

In a children's playground game, four light inextensible ropes are attached at one end to a small toy ring.

Four children each take the other end of a rope and pull it taut.

The ring is in equilibrium and the whole system is in a horizontal plane with appropriate axes as shown in the diagram.

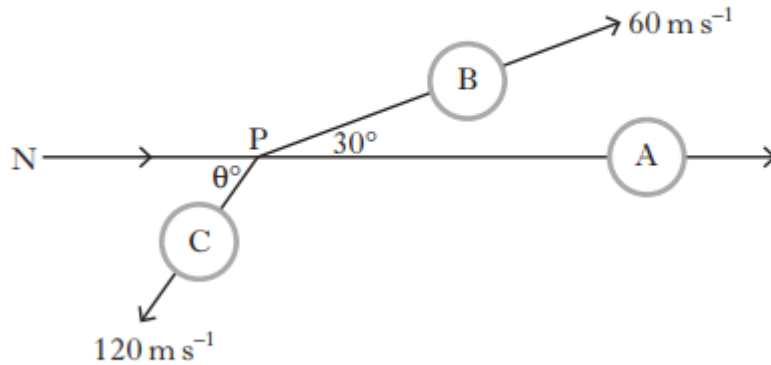


The tensions in the four ropes are P , Q , 80 and 64 newtons respectively, and their directions relative to the axes are shown.

Calculate the magnitude of the tensions P and Q .

4

A shell of mass 20 kg is travelling in a horizontal plane along the line NP at 100 m s^{-1} . At P it breaks into 3 pieces A , B and C of masses 12 kg , 6 kg and 2 kg respectively. These pieces instantaneously travel as shown in the diagram.



Find the speed of A , and the size of angle θ° .

4

An automated train is programmed to move from rest under constant acceleration to a maximum speed of 20 m s^{-1} in a distance of 300 m . It is brought to rest under uniform deceleration in 15 seconds . Two stations are 5 kilometres apart and the train is programmed to stop at each station.

Find the time taken to travel between the two stations.

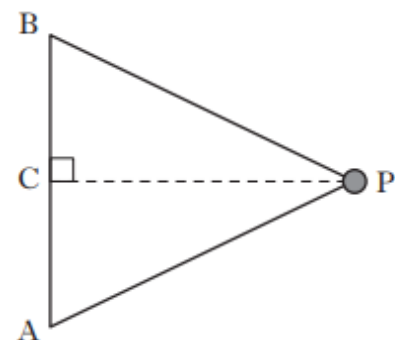
5

A catapult consists of an elastic string of natural length 40 cm and modulus of elasticity 25 N . One end of the string is fixed to A and the other to B , with AB of length 20 centimetres .

A particle of mass 20 g is held in the middle of the string and the string pulled back to P .

It is held at rest with PC of length 24 centimetres . A , B , P and C all lie on the same horizontal plane. The particle is then released.

Find the speed with which it passes through C .



5

Two particles, P and Q , of masses 2 kg and $m\text{ kg}$ respectively, initially lie at rest in a straight line on a smooth horizontal surface. Particle P is acted on by a constant force of 3 N for 4 seconds , causing it to accelerate towards Q . When P collides with Q the particles coalesce and begin to move with speed 3.75 m s^{-1} .

Find the value of m , the mass of particle Q .

4

<p>An object oscillates on the x-axis about the origin, O, with simple harmonic motion. The period of the oscillation is $\frac{14\pi}{5}$ seconds, and when the object is at point K, 1.2 metres from the origin, it is moving away from the origin with a velocity of 2.5 m s^{-1}.</p> <p>Find the amplitude of the motion and the time it takes for the particle to travel from O to K.</p>	4
<p>A particle is moving in a plane such that t seconds after the start of its motion, the velocity is given by $(3t\mathbf{i} + 5t^2\mathbf{j}) \text{ m s}^{-1}$.</p> <p>The particle is initially at the point $\left(\frac{1}{2}\mathbf{i} - 7\mathbf{j}\right)$ metres relative to a fixed origin O.</p> <p>Find the distance of the particle from O when $t = 3$.</p>	3
<p>A ball of mass 0.5 kg is released from rest at a height of 10 metres above the ground.</p> <p>If the ball reaches 2.5 metres after its first bounce, calculate the size of the impulse exerted by the ground on the ball.</p>	4

Ans: $v=13.8\text{ms}^{-1}$, $v=8.143\text{ms}^{-1}$, $P=101\text{N}$, $Q=95.4\text{N}$, $v=154\text{ms}^{-1}$, $\theta=48.6^\circ$, $t=272.5\text{s}$, $v=6.71\text{ms}^{-1}$, $m=1.2\text{kg}$, $t=0.46\text{s}$, $s=40.5\text{m}$, $l=10.5\text{Ns}$.

There are 40 marks available at C level.

Grade Booster 2 will focus on the pure maths.