

## Homework 12 solutions

1) Conservation of momentum

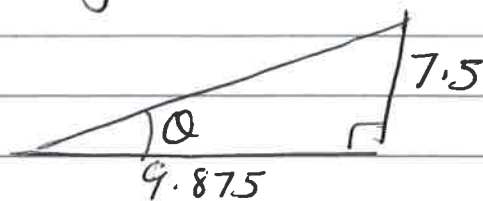
momentum before = momentum after

$$1200 \times 18 \underline{i} + 2000(5 \underline{i} + 12 \underline{j}) = 3200 \underline{v}$$

$$31600 \underline{i} + 24000 \underline{j} = 3200 \underline{v}$$

$$\underline{v} = 9.875 \underline{i} + 7.5 \underline{j}$$

$$|\underline{v}| = \sqrt{9.875^2 + 7.5^2}$$
$$= 12.4 \text{ ms}^{-1}$$



$$\tan \theta = \frac{7.5}{9.875}$$

$$\theta = 37.2^\circ \text{ to the x-axis.}$$

2) Particle P

$$u = 0$$

$$t = 4 \text{ sec}$$

$$a = \frac{F}{m}$$

$$a = \frac{3}{2}$$

$$v = u + at$$

$$v = 0 + \frac{3}{2} \times 4$$

$$\underline{v = 6 \text{ ms}^{-1}}$$

momentum before = momentum after

$$2 \times 6 + m \times 0 = (2 + m) \times 3.75$$

$$12 = 7.5 + 3.75m$$

$$\underline{m = 1.2 \text{ kg}}$$

3) momentum before = momentum after

$$1 \times (-2\mathbf{i} + 4\mathbf{j}) + 2\mathbf{v} = 3 \times (\mathbf{i} + 4\mathbf{j}) \checkmark$$

$$-2\mathbf{i} + 4\mathbf{j} + 2\mathbf{v} = 3\mathbf{i} + 12\mathbf{j}$$

$$2\mathbf{v} = 5\mathbf{i} + 8\mathbf{j}$$

$$\mathbf{v} = \left(\frac{5}{2}\mathbf{i} + 4\mathbf{j}\right) \text{ms}^{-1} \checkmark$$

$$|\underline{v}| = \sqrt{\left(\frac{5}{2}\right)^2 + 4^2}$$

$$= \underline{4.72 \text{ms}^{-1}} \checkmark$$

4) Impulse = change in momentum

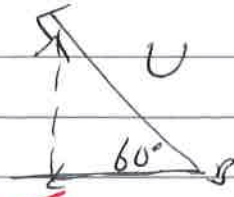
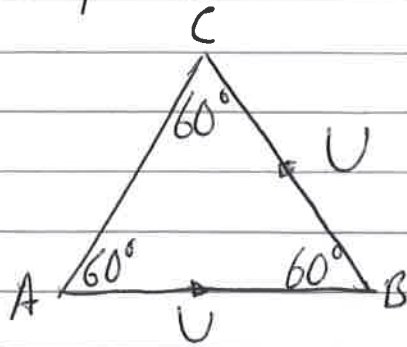
$$I = \int F dt$$

$$I = \int_0^1 100 \cos\left(\frac{1}{2}\pi\right)t dt \checkmark$$

$$I = \left[\frac{100}{\frac{1}{2}\pi} \sin\left(\frac{1}{2}\pi\right)t\right]_0^1 \checkmark$$

$$I = \underline{63.7 \text{Ns}} \checkmark$$

b) one possible solution



$$A \rightarrow B \quad \text{momentum} = mU \underline{i}$$

$$B \rightarrow C \quad \text{momentum} = m(-U \cos 60 \underline{i}) + m(U \sin 60 \underline{j}) \\ = -\frac{1}{2} mU \underline{i} + \frac{\sqrt{3}}{2} mU \underline{j}$$

Impulse = change in momentum

$$= -\frac{1}{2} mU \underline{i} + \frac{\sqrt{3}}{2} mU \underline{j} - mU \underline{i}$$

$$= -\frac{3}{2} mU \underline{i} + \frac{\sqrt{3}}{2} mU \underline{j}$$

$$|I| = \sqrt{\left(\frac{3}{2} mU\right)^2 + \left(\frac{\sqrt{3}}{2} mU\right)^2}$$

$$= \sqrt{\frac{9}{4} m^2 U^2 + \frac{3}{4} m^2 U^2}$$

$$= \sqrt{3 m^2 U^2}$$

$$= \underline{\underline{\sqrt{3} mU \text{ Ns}}}$$

$$5) \quad I = \int F dt$$

$$I = \int_0^6 (4t\mathbf{i} - 2t\mathbf{j}) dt \quad \checkmark$$

$$I = [2t^2\mathbf{i} - 2t\mathbf{j}]_0^6$$

$$I = (72\mathbf{i} - 12\mathbf{j}) \text{ Ns} \quad \checkmark$$

$$I = mv - mu$$

$$72\mathbf{i} - 12\mathbf{j} = 3v - 3(3\mathbf{i} + \mathbf{j}) \quad \checkmark$$

$$72\mathbf{i} - 12\mathbf{j} = 3v - 9\mathbf{i} - 3\mathbf{j}$$

$$3v = 81\mathbf{i} - 9\mathbf{j}$$

$$v = (27\mathbf{i} - 3\mathbf{j}) \text{ ms}^{-1} \quad \checkmark$$

$$\text{speed} = |v| = \sqrt{27^2 + 3^2} = \underline{\underline{27.2 \text{ ms}^{-1}}} \quad \checkmark$$