| Υ  | Q  | Momentum and Impulse  |   |
|----|----|---|---|
| 24 | 3  | Particle A has a mass of 30 grams and is travelling in a straight line with velocity $u  \text{m s}^{-1}$ .   |   |
|    |    | It collides with a stationary particle B and rebounds with a speed of $\frac{u}{3}$ ms <sup>-1</sup> in the opposite direction.   |   |
|    |    | Particle B begins to move with a velocity of $\frac{u}{2}$ ms <sup>-1</sup> in the original direction of motion.  |   |
|    |    | Calculate the mass of particle B.   | 3 |
| 23 | 1  | An air hockey pusher of mass 48 grams is moving freely with a velocity of 16i cms <sup>-1</sup> when it collides with a stationary puck of mass 32 grams.   |   |
|    |    | Immediately after the collision the pusher has a velocity of $(4i-8j)$ cms <sup>-1</sup> .  |   |
|    |    |   |   |
|    |    | Calculate the magnitude of the velocity of the puck immediately after the collision.  | 3 |
| 23 | 15 | A bullet of mass $m$ kg is fired at a block of wood of mass $M$ kg which hangs vertically and at rest at the end of a light inextensible string.  |   |
|    |    | The bullet enters the block horizontally while travelling at a speed of $u  {\rm m  s^{-1}}$ , and becomes embedded in the block.   |   |
|    |    | The block then swings until it reaches a height $h$ metres above its original position.   |   |
|    |    | Show that $h = \frac{1}{2g} \left( \frac{mu}{M+m} \right)^2$ .  | 5 |
| 22 | 1  | An object of mass 8 kg is at rest on a smooth horizontal surface. A constant horizontal force of magnitude 65 newtons is applied for 1.2 seconds.   |   |
|    |    | (a) Calculate the speed of the object after this time.  | 2 |
|    |    | The object then hits a wall and rebounds in the opposite direction with no loss of energy.  |   |
|    |    | (b) Calculate the magnitude of the impulse of the wall on the object.   | 2 |
| 19 | 1  | A body of mass 4 kg is moving with initial velocity $(3i+2j)$ ms <sup>-1</sup> . It is given an impulse of $(6i+j)$ Ns.   |   |
|    |    | Calculate the magnitude of the final velocity and the angle it makes with the $x$ -axis.  | 4 |
| 18 | 3  | An object of mass $10  \text{kg}$ is projected along a rough horizontal surface with an initial speed of $12  \text{m s}^{-1}$ . The coefficient of friction between the object and the surface is $0.25$ . |   |
|    |    | After travelling a distance of 20 metres along this rough surface it collides and coalesces with a stationary object of mass 5 kg.  |   |
|    |    | Find the speed of the combined objects immediately after the collision.   | 5 |

| 18       | 17 | A box of mass $m \log s$ is set in motion with an initial impulse $I$ . As it moves along the surface it experiences a resistive force proportional to the square of its velocity $v \operatorname{ms}^{-1}$ .      |             |
|----------|----|---|-------------|
|          |    | By setting up a differential equation, show that the velocity of the box after $t$ seconds can be expressed as $v = \frac{mI}{Ikt + m^2}$ , where $k$ is a constant and $t$ is measured from the moment of impulse. | 5           |
| 17       | 8  | Two particles, X and Y, have masses of $0.2  \text{kg}$ and $0.5  \text{kg}$ respectively.  | <del></del> |
|          |    | They are moving up a smooth plane AB, inclined at $30^{\circ}$ to the horizontal as shown in the diagram.   |             |
|          |    | В   |             |
|          |    | X Y   |             |
|          |    | A   |             |
|          |    | The particles collide $3.5$ metres from B when X is moving with a speed of $6 \mathrm{ms^{-1}}$ and Y is moving with a speed of $3 \mathrm{ms^{-1}}$ .  |             |
|          |    | This collision causes X to come instantaneously to rest while Y continues to travel up the slope.   |             |
|          |    | Show that in the subsequent motion, Y comes to rest before reaching B.  | 6           |
| 16       | 1  | A bicycle and rider have a total mass of 70 kg. They are travelling at $12\mathrm{ms^{-1}}$ . The cyclist applies the brakes for 1.5 seconds, resulting in a total resistive force of 180 newtons.                  |             |
|          |    | What is the speed of the bicycle after 1.5 seconds?   | 3           |
| 16<br>Sp | 1  | A curling stone, P, of mass 18 kg is moving with velocity $\begin{pmatrix} 0 \\ -1 \cdot 1 \end{pmatrix}$ m s <sup>-1</sup> relative to a   |             |
|          |    | suitable set of coordinate axes. It collides with a stationary curling stone, Q, of   |             |
|          |    | mass 20 kg. Q then moves off with velocity $\begin{pmatrix} 0.36 \\ -0.72 \end{pmatrix}$ m s <sup>-1</sup> .  |             |
|          |    | Calculate the speed with which P travels immediately after impact.  | 3           |
|          |    |   |             |