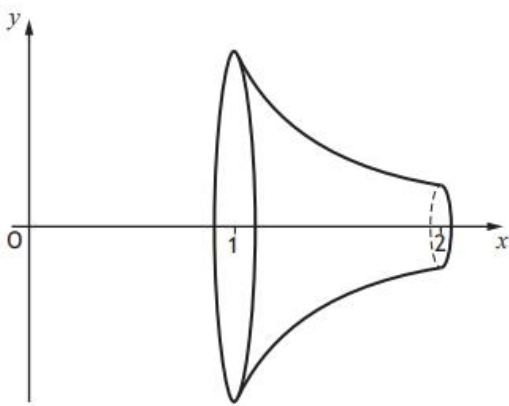
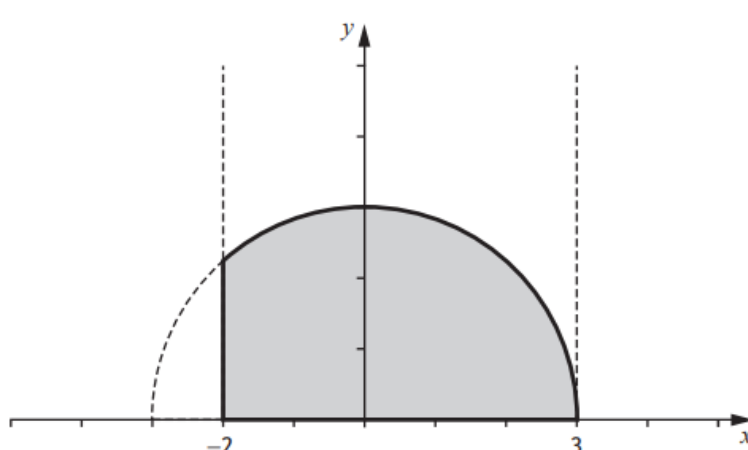
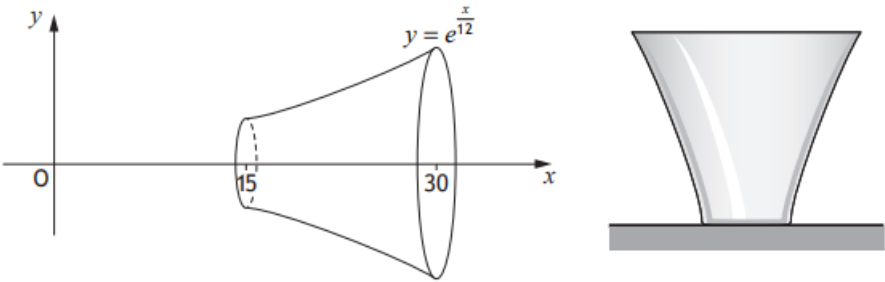
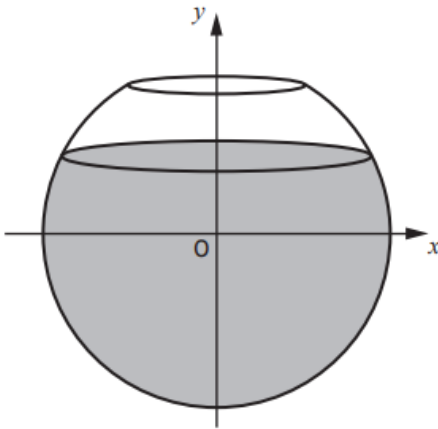


Y	Q	Volume of Revolution
2023	17	<p>(a) Use integration by parts to find $\int x \sin 2x \, dx$. 3</p> <p>A solid is formed by rotating the curve with equation $y = \sqrt{x \sin 2x}$ between $x = 0$ and $x = 1$ through 2π radians about the x-axis.</p> <p>(b) Calculate the volume of this solid. 3</p>
2022	9	<p>An object is formed by rotating the curve $y = \frac{6x}{3x^3 - 1}$ between $x = 1$ and $x = 2$, through 2π radians about the x-axis.</p> <div style="text-align: center;">  </div> <p>Using the substitution $u = 3x^3 - 1$, or otherwise, find the exact value of the volume of this object. 6</p>
2018	6	<p>A part of the graph of $x^2 + y^2 = 9$ is shown in the diagram below.</p> <div style="text-align: center;">  </div> <p>The shaded area is bounded by the graph, the x-axis and the lines $x = -2$ and $x = 3$. This area is rotated 360° about the x-axis.</p> <p>Calculate the volume of the solid formed by this rotation. 4</p>

2016	13	<p>A glass bowl is modelled by rotating the curve $y = e^{\frac{x}{12}}$ between $x=15$ and $x=30$ through 2π radians about the x-axis as shown in the diagram.</p>  <p>(a) Find the volume of the bowl. 3</p> <p>(b) A line is to be put on the bowl to indicate when it is half full. How far above the base of the bowl should this line be marked? 3</p>
2016 Spec	11	<p>A flower vase is modelled by rotating part of the curve $x = \sqrt{100 - y^2}$ through 2π radians about the y-axis as shown in the diagram.</p>  <p>(a) Find the volume of water needed to fill the vase to a depth of 16 cm. 4</p> <p>(b) State one improvement that could be made to the design 1</p>