# September Revision Booklet S5/6 National 5 

Volume of a sphere:

$$
V=\frac{4}{3} \pi r^{3}
$$

Volume of a cone:

$$
V=\frac{1}{3} \pi r^{2} h
$$

Volume of a pyramid:

$$
V=\frac{1}{3} A h
$$

| Textbook revision for the September Assessment |  |  |
| :--- | :--- | :--- |
|  | TJ Nat 5 | Leckie \& Leckie Nat 5 |
| Surds | Pg 171 Q2\&7, | Pg 5 Q3\&4 Page 6 Q1\&2 |
| Indices | Pg 175 Q6, 7 \&111 | Pg 18 Q2, Pg 19 Q3 |
| Standard Form | Pg 5 Q47 | Pg 24 Q2-5 |
| Expanding Brackets | P15 Q3, Pg 16 Q6\&7 | Pg 32 Q2, Pg 33 Q2 |
| Factorising | P66 Q1, P67 Q2 | Pg 37 Q3, Pg 40 Q3 |
| Completing the square | Pg 187 Q2,3 | Pg 43 Q3 |
| Numerical Fractions | Pg 32 Q1-3 | Pg 341 Q1\&2, Pg 342 Q1\&2 |
| Algebraic Fractions | Pg 96 Q2,3\&4 | Pg 49 Q2, Pg 55 Q2, <br> Pg 56 Q1, Pg 58 Q1 |
| Arcs and Sectors of Circles | Pg 126 Q4, Pg 127 Q4 | Pg 70 Q1, Pg 74 Q1 |
| Volume of 3D solids | Pg 8 Q74-76 | Pg 77 Q1\&2, Pg 81 Q1, <br> Pg 82 Q1 \&4 |
| Percentage change | Pg 26 Q4.5\%8 | Pg 331 Q4-7 |
| Reverse Percentages | Pg 27 Q1,2\&7 | Pg 335 Q3-6 |


| Maths workout revision for the September Assessment <br> https://www.mathsworkout.co.uk/ <br> Login madras col <br> password value28 |  |
| :---: | :---: |
| Surds | Number Topic 20 <br> - Simplifying a surd <br> - Simplify a Product of Surds 1 <br> - Simplifying a Sum or Difference of Surds 1 |
| Indices | Number Topic 19 <br> - Multiplying and Dividing Indices (2 tasks) <br> - Raising a Power to a Power <br> - Simplifying Expressions 1 <br> - Converting between Fractional Indices and Surds |
| Standard Form | Number Topic 21 - All 4 Level 5 tasks |
| Expanding Brackets, Factorising Completing the square | Algebra Topic 12 <br> - Expanding Brackets <br> - Factorising Quadratics <br> - The difference of Two Squares <br> - Completing the Square |
| Numerical Fractions | Number Topic 14 <br> - Improper Fractions 1 <br> - Adding and Subtracting Fractions 3 (2 tasks) <br> - Multiplying and Dividing Fractions 2 (2 tasks) |
| Algebraic Fractions | Algebra Topic 13 <br> - A few slides from each of the four tasks |
| Arcs and Sectors of Circles | Geometry and Measures Topic 21 <br> - Calculating Arcs and Calculating Sectors (2 tasks) |
| Volume of 3D solids | Geometry and Measures Topic 15 <br> - Volume of a Cylinder, Cone and Sphere (3 tasks) |
| Percentage change over time and reverse percentages. | Ratio, Proportion and Rates of Change Topic 7 <br> - Calculating Compound Interest 1 and 2 <br> - Calculating Reverse Percentage |


| A | S5 Nat 5 September Revision Non-Calculator | 15 |
| :---: | :---: | :---: |
| 1 | Evaluate $1 \frac{2}{7}+\frac{5}{6}$ | 2 |
| 2 | Multiply out the brackets and collect like terms $(2 x+3)(x-5)$ | 2 |
| 3 | Factorise $\quad x^{2}+12 x+11$ | 2 |
| 4 | (a) Simplify $3^{0}$ <br> (b) Write $\sqrt{5}$ in index form. <br> (c) Hence calculate $100^{\frac{1}{2}}$ | $1$ <br> 1 <br> 2 |
| 5 | Simplify $\frac{2}{b^{2}} \times \frac{3 b}{4}$ | 2 |
| 6 | simplify $\frac{(x+3)^{2}}{x^{2}+5 x+6}$ | 3 |
| A | S5 Nat 5 September Revision Calculator | 15 |
| 7 | There are 984 pupils on the school roll for Banchory High School. It is forecast that the school roll will decrease by $10 \%$ per year for the next three years. <br> What is the expected school roll after three years? <br> Give your answer rounded to two significant figures. | 4 |
| 8 | Write $x^{2}+10 x+12$ in completed square form $(x+p)^{2}+q$ | 2 |
| 9 | Simplify $10 a^{6} b^{3} \times 4 a^{2} b^{-2}$ | 3 |


| 10 | The diagram shows a sector of a circle. <br> The radius of the circle is 85 cm and the centre <br> angle is $78^{\circ}$. <br> Calculate the length of the arc for this sector. | Calculate the volume of a sphere with a radius <br> of 22 centimetres <br> Give your answer rounded to the nearest <br> thousand |
| :--- | :--- | :--- |
| $\mathbf{1 1}$ |  | 3 |


| Answers to Revision Paper A |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Non-Calculator |  | Calculator |
| 1 | $\begin{gathered} \left(\frac{2}{7}+\frac{5}{6}\right)=\left(\frac{12}{42}+\frac{35}{42}\right)=\frac{47}{42}=1 \frac{5}{42} \\ 1+1 \frac{5}{42}=2 \frac{5}{42} \end{gathered}$ | 7 | $\begin{gathered} 984 \times 0.9^{3}=717.336 \\ \mathbf{7 2 0} \text { pupils } \end{gathered}$ |
| 2 | $\begin{gathered} (2 x+3)(x-5) \\ =2 x^{2}-10 x+3 x-15 \\ =2 x^{2}-\mathbf{7 x}-\mathbf{1 5} \end{gathered}$ | 8 | $\begin{gathered} x^{2}+10 x+12=(x+5)^{2}+12-25 \\ =(\boldsymbol{x}+\mathbf{5})^{2}-\mathbf{1 3} \end{gathered}$ |
| 3 | $x^{2}+12 x+11=(x+11)(x+1)$ | 9 | $10 a^{6} b^{3} \times 4 a^{2} b^{-2}=40 \boldsymbol{a}^{6} \boldsymbol{b}$ |
| 4 | $\begin{gathered} 3^{0}=\mathbf{1} \\ \sqrt{5}=5^{\frac{1}{2}} \\ 100^{\frac{1}{2}}=\sqrt{100}=\mathbf{1 0} \end{gathered}$ | 10 | $A r c=\frac{78}{360} \times \pi \times 2 \times 85=115.7 \mathbf{c m}$ |
| 5 | $\frac{2}{b^{2}} \times \frac{3 b}{4}=\frac{6 b}{4 b^{2}}=\frac{3}{2 b}$ | 11 | $\begin{aligned} V= & \frac{4}{3} \times \pi \times 22^{3}=44602.2381 \\ & \text { Volume is } \mathbf{4 5 0 0 0} \mathbf{~ c m}^{3} \end{aligned}$ |
| 6 | $\frac{(x+3)(x+3)}{(x+2)(x+3)}=\frac{\boldsymbol{x}+\mathbf{3}}{\boldsymbol{x}+\mathbf{2}}$ |  |  |


| B | S5 Nat 5 September Revision Non-Calculator | 13 |
| :---: | :---: | :---: |
| 1 | Evaluate $1 \frac{3}{7} \times \frac{2}{5}$ | 2 |
| 2 | Multiply out the brackets and collect like terms $(3 x-1)^{2}+5 x$ | 3 |
| 3 | Write $x^{2}-4 x+11$ in completed square form $(x+p)^{2}+q$ | 2 |
| 4 | Factorise $2 x^{2}-18$ | 2 |
| 5 | Simplify $m^{7} \times m^{3} \div m^{-6}$ | 2 |
| 6 | Simplify $\sqrt{12} \times \sqrt{3}$ | 2 |
| B | S5 Nat 5 September Revision Calculator | 17 |
| 7 | The population of Dundee is increasing at a steady rate of $1.7 \%$ per year. <br> At present the population is 148300 . <br> What is the expected population in five years time? | 3 |
| 8 | The diagram shows a sector of a circle. <br> The radius of the circle is 6 metres and the centre angle is $185^{\circ}$. <br> Calculate the area of this sector. | 3 |
| 10 | An insect weighs $3.82 \times 10^{-2}$ grams. One day it consumes 5 times its weight in food. How much food does it eat? Give your answer in scientific notation. | 2 |


| $\mathbf{9}$ |  | Calculate the volume of a cone with a <br> diameter of 32 centimetres and a height of 46 <br> centimetres. <br> Give your answer correct to 2 significant <br> figures. |
| :--- | :--- | :--- |
| $\mathbf{1 1}$ | The price of Bella’s summer holiday is $£ 924$. <br> What is the price of the holiday without the booking fee? | $\mathbf{3}$ |
| $\mathbf{1 2}$ | Express $\frac{3}{x}+\frac{4}{x+1}, x \neq 0, x \neq-1$ as a single fraction in the simplest form | $\mathbf{3}$ |


| Answers to Revision Paper B |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Non-Calculator |  | Calculator |
| 1 | $1 \frac{3}{7} \times \frac{2}{5}=\frac{10}{7} \times \frac{2}{5}=\frac{20}{35}=\frac{4}{7}$ | 7 | $148300 \times 1.017^{5}=161341$ |
| 2 | $\begin{gathered} (3 x-1)^{2}=(3 x-1)(3 x-1) \\ =9 x^{2}-3 x-3 x+1 \\ (3 x-1)^{2}+5 x=9 x^{2}-x+1 \end{gathered}$ | 8 | $\begin{aligned} & \text { Area }=\frac{185}{360} \times \pi \times 6^{2} \\ & \text { Area }=58.12 \mathrm{~cm}^{2} \end{aligned}$ |
| 3 | $\begin{gathered} (x-2)^{2}+11-2^{2} \\ (x-2)^{2}+7 \end{gathered}$ | 9 | $\begin{gathered} 3.82 \times 10^{-2} \times 5=0.191 \\ 1.91 \times \mathbf{1 0}^{-\mathbf{1}} \text { grams } \end{gathered}$ |
| 4 | $\begin{gathered} x^{2}-16=(\boldsymbol{x}+4)(\boldsymbol{x}-4) \\ 2 x^{2}-18=2\left(x^{2}-9\right) \\ =2(\boldsymbol{x}-3)(\boldsymbol{x}+3) \end{gathered}$ | 10 | $\begin{gathered} V=\frac{1}{3} \times \pi \times 16^{2} \times 46=12331.798 \ldots \\ V=12000 \mathbf{c m}^{3} \end{gathered}$ |
| 5 | $\begin{gathered} m^{7} \times m^{3} \div m^{-6} \\ =m^{10} \div m^{-6} \\ =\boldsymbol{m}^{16} \end{gathered}$ | 11 | $\begin{gathered} 105 \%=£ 924 \\ 1 \%=924 \div 105=8.8 \\ \mathbf{1 0 0} \%=£ \mathbf{8 8 0} \end{gathered}$ |
| 6 | $\sqrt{12} \times \sqrt{3}=\sqrt{36}=6$ | 12 | $\frac{3(x+1)+4 x}{x(x+1)}=\frac{\mathbf{7 x}+\mathbf{3}}{\boldsymbol{x}(\boldsymbol{x}+\mathbf{1})}$ |


| $\mathbf{C}$ | S5 Nat 5 September Revision Non-Calculator | $\mathbf{1 4}$ |
| :--- | :--- | :---: |
| $\mathbf{1}$ | Evaluate $\frac{1}{3} \div 2 \frac{2}{3}$ | $\mathbf{2}$ |
| $\mathbf{2}$ | Factorise $x^{2}-4 x-21$ | $\mathbf{2}$ |
| $\mathbf{3}$ | Multiply out the brackets and collect like terms $\quad(4 x-7)(2 x+1)$ <br> The radius of the circle is 20 mm and the angle at <br> the centre is $45^{\circ}$. <br> Without a calculator and using $\pi=3.14$, find <br> the length of the arc for this sector. | $\mathbf{2}$ |
| $\mathbf{4}$ | The diagram shows a sector of a circle. | $\mathbf{3}$ |
| $\mathbf{5}$ | Simplify $\sqrt{50}-\sqrt{2}$ | $\mathbf{2 0}$ mm |


| 10 | A shape is made by placing a cone on top of a hemisphere. <br> The hemisphere has a radius of 6 cm . <br> The cone has a radius of 6 cm and a height of 10 cm . <br> Calculate the volume of this shape. | 4 |
| :---: | :---: | :---: |
| 12 | (a) Factorise <br> (i) $x^{2}+5 x+4$ <br> (ii) $x^{2}-16$ <br> (b) Hence simplify $\frac{x^{2}+5 x+4}{x^{2}-16}$ | 2 2 |
|  | 30 marks |  |


| Answers to Revision Paper C |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Non-Calculator |  | Calculator |
| 1 | $\frac{1}{3} \div 2 \frac{2}{3}=\frac{1}{3} \div \frac{8}{3}=\frac{1}{3} \times \frac{3}{8}=\frac{1}{8}$ | 7 | $\begin{gathered} 30000 \times(1-0.11)^{4} \\ 30000 \times(0.89)^{4}=£ 18822.6723 \\ £ 18823 \\ \hline \end{gathered}$ |
| 2 | $x^{2}-4 x-21=(x-7)(x+3)$ | 8 | $\begin{gathered} (x-6)^{2}+21-6^{2} \\ (x-6)^{2}-15 \end{gathered}$ |
| 3 | $\begin{gathered} 8 x^{2}+4 x-14 x-7 \\ 8 \boldsymbol{x}^{2}-\mathbf{1 0 x}-\mathbf{7} \end{gathered}$ | 9 | $f^{5} \times f^{6}=\boldsymbol{f}^{11}$ |
| 4 | $\begin{gathered} \text { Arc }=\frac{45}{360} \times 3.14 \times 40 \\ \text { Arc }=\frac{1}{8} \times 40 \times 3.14 \\ \text { Arc }=5 \times 3.14 \\ \text { Arc }=\mathbf{1 5 . 7} \mathbf{~ c m} \end{gathered}$ | 10 | Volume of the cone is $V=\frac{1}{3} \times \pi \times 6^{2} \times 11=414.690 \ldots$ <br> Volume of the hemisphere is $V=\frac{4}{3} \times \pi \times 6^{3} \div 2=452.389 \ldots$ <br> Volume of the shape is $\mathbf{8 6 7} \mathbf{c m}^{\mathbf{3}}$ |
| 5 | $\begin{gathered} \sqrt{50}-\sqrt{2}=\sqrt{25} \sqrt{2}-\sqrt{2} \\ =5 \sqrt{2}-\sqrt{2}=4 \sqrt{2} \end{gathered}$ | 11 | $=\frac{(x+4)(x+1)}{(x+4)(x-4)}=\frac{x+1}{x-4}$ |
| 6 | $\begin{gathered} \hline 90 \%=270 \quad 10 \%=270 \div 9=30 \\ \mathbf{1 0 0} \%=\mathbf{3 0 0} \end{gathered}$ |  |  |

