

2009 Mathematics

Standard Grade Credit

Finalised Marking Instructions

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Special Instructions

1 The main principle in marking scripts is to give credit for the skills which have been demonstrated. Failure to have the correct method may not preclude a pupil gaining credit for the calculations involved or for the communication of the answer.

Care should be taken to ensure that the mark for any question or part question is entered in the correct column, as indicated by the horizontal line.

Where a candidate has scored zero marks for any question attempted, "0" should be shown against the answer in the appropriate column.

It is of great importance that the utmost care should be exercised in adding up the marks. Where appropriate, all summations for totals and grand totals must be carefully checked.

- 2 The answer to one part, correct **or incorrect** must be accepted as a basis for subsequent dependent parts of a question. Full marks in the dependent part is possible if it is of equivalent difficulty.
- 3 Do not penalise insignificant errors. An insignificant error is one which is significantly below the level of attainment being assessed.
 - eg An error in the calculation of 16 + 15 would not be penalised at Credit Level.
- 4 Working after a correct answer should **only** be taken into account if it provides **firm** evidence that the requirements of the question have not been met.
- 5 In certain cases an error will ease subsequent working. **Full** credit cannot be given for this subsequent work but **partial** credit may be given.
- 6 Accept answers arrived at by inspection or mentally, where it is possible for the answer to have been so obtained.
- 7 Do not penalise omission or misuse of units unless marks have been specifically allocated to units.

8 A wrong answer without working receives no credit unless specifically mentioned in the marking scheme.

The rubric on the outside of the Papers emphasises that working must be shown. In general markers will only be able to give credit to partial answers if working is shown. However there may be a few questions where partially correct answers unsupported by working can still be given some credit. Any such instances will be stated in the marking scheme.

9 Acceptable alternative methods of solution can only be given the marks specified, ie a more sophisticated method cannot be given more marks.

Note that for some questions a method will be specified.

- 10 In general do not penalise the same error twice in the one question.
- 11 Accept legitimate variations in numerical/algebraic questions.
- 12 Do not penalise bad form eg sin $x^{\circ} = 0.5 = 30^{\circ}$.
- 13 A transcription error is not normally penalised except where the question has been simplified as a result.

2009 Mathematics SG – Credit Level – Paper 1

Draft Marking Instructions

Award marks in whole numbers only

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
1	Ans: 27.11	
	• division	• 28.2
	• subtraction	• 27.11 2KU
NOTES:	<u>.</u>	

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
2	 Ans: 2⁵/₆ common denominator fraction 	• $4\frac{2}{6} - 1\frac{3}{6}$ • $\frac{17}{6}$ 2KU
NOTES:		

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
3 (a)	Ans: 19	
	• substitution	• $(-4)^2 + 3$
	• evaluation	• 19 2KU
NOTES:		
(i)	for 19, with or without working	award 2/2
(b)	Ans: $t = \pm 7$	
	• substitution	• $t^2 + 3 = 52$
	• evaluation	• $t = \pm 7$ 2RE
NOTES: (i)	for ± 7 , with or without working	award 2/2
(ii)	for 7 or -7 , with or without working	award 1/2

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
4 (a)	Ans: $(x-2y)(x+2y)$ • factorising	• $(x-2y)(x+2y)$
		1KU
NOTES:		
(b)	Ans: $2x^2 + 7x - 4$ • expansion	• $2x^2 + 7x - 4$ 1KU
NOTES:	1	1
(c)	 Ans: 3x^{3/2} + x^{-3/2} a correct term a second correct term with no further 'simplification' 	• $3x^{\frac{3}{2}}$ or $x^{-\frac{3}{2}}$ • $3x^{\frac{3}{2}}$ or $x^{-\frac{3}{2}}$ 2KU
NOTES: (i) (ii)	accept indices in decimal form a further 'simplification' could be $3x^{\frac{3}{2}} + x^{-\frac{3}{2}}$	$=3x^0$

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
5	Ans: $4\sqrt{3}$	
	• method	• $BC^2 = 8^2 - 4^2$
	• processing	• $\sqrt{48}$
	• simplification	• 4 √3
		3 KU
NOTES:		

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
6	Ans: P(female) plus justification	
	• probability (female)	• $\frac{4}{18}$
	• probability (5)	• $\frac{1}{6}$
	• communication	• female (with justification)
		3RE
NOTES:		
(i)	for the 3 rd mark, justification must show	
	(a) both probabilities with same numerator	or or denominator
	and	
	(b) a consistent decision	

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
7	Ans: £200	
	• valid strategy	• 130% = 260
	• processing	• $100\% = \frac{260}{1.3}$
	• solution	• 200 3KU
NOTES:		
(i)	for £200, with or without working	award 3/3
(ii)	for £371.43 (70% = £260), with working	award 2/3
(iii)	for £338 (130% of £260), with or without wo	rking award 0/3
(iv)	for £182 (70% of £260), with or without work	king award 0/3
(v)	caution: some candidates state $130\% = \pounds 2$ (iii) or (iv); in these cases, the 1^{st}	60 and follow this as note mark is still available

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
8 (a)	Ans: $6x + 2y = 42$	
	• starting to form equation	• $x+5x+2y$
	• equation	• $x + 5x + 2y = 42$ 2KU
NOTES:		
	1	
(b)	Ans: $5x - 2y = 2$	
	• starting to form equation	• an equation containing only the terms 5 <i>x</i> , 2 <i>y</i> and 2
	• equation	• $5x - 2y = 2$
NOTES:		
	Ι	Ι
(c)	Ans: $x = 4, y = 9$	
	• method	• $11x = 44$ or equivalent
	• processing	• <i>x</i> = 4
	• processing	• $y = 9$
NOTES		JAL
(i)	for 4 and 9 verified in both equations	award 1/3

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
9	Ans: $d = \sqrt{\frac{20f}{k}}$	
	• beginning to rearrange	• $kd^2 = 20f$
	continuing rearrangement	• $d^2 = \frac{20f}{k}$
	• completed rearrangement	• $d = \sqrt{\frac{20f}{k}}$
		3KU
NOTES:		
(i)	for $d = \sqrt{\frac{20f}{k}}$, with or without working	award 3/3
(ii)	for $d = \frac{\sqrt{20f}}{k}$, with or without working	award 2/3
(iii)	the 3 rd mark is for the square root of the candi	date's expression for d^2

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
10 (a)	Ans: 14 seconds	
	• strategy	$\bullet -2t(t-14)=0$
	• solution	• 14 2RE
NOTES:		
(i)	for an answer of 14 with no working	award 2/2
(ii)	caution: an answer of 14 may be the result ensure that working is valid	of incorrect working:
(b)	Ans: 98 metres	
	• method	• $(x=)7$
	• solution	• 98 2RE
NOTES:		

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
11	Ans: 0.3	
	• correct use of sine rule	• $\frac{10}{\sin 30^\circ} = \frac{6}{\sin A}$
	• rearranging	• $\sin A = \frac{6\sin 30^\circ}{10}$
	• simplification	• 0.3 3RE
NOTES: (i)	candidates who assume that $\sin A = 0.3$ may be	be awarded a maximum of $\frac{1}{3}$ (1 st mark)

KU 21 marks RE 17 marks

[END OF PAPER 1 MARKING INSTRUCTIONS]

2009 Mathematics SG – Credit Level – Paper 2

Marking Instructions

Award marks in whole numbers only

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
1	Ans: 3.1×10^{24}	
	• method	• $\frac{1000}{3.27 \times 10^{-22}}$
	• processing	• 3.058×10^{24}
	• rounding	• 3.1×10^{24}
		3 KU
NOTES:		
(i)	3.1×10^{24} with or without working	award 3/3
(ii)	3.06×10^{24} with or without working	award 2/3
(iii)	$3.058 \times 10^{24} \rightarrow 3.05 \times 10^{24}$	award 2/3
(iv)	3.05×10^{24} without working	award 1/3
(v)	$1000 \times 3.27 \times 10^{-22} \rightarrow 3.3 \times 10^{-19}$	award 1/3
(vi)	3.1×10^{n} [<i>n</i> = 21, 22, 23] without working	award 1/3
(vii)	3.3×10^{-19} without working	award 0/3
(viii)	for any other final answer, an unrounded solu	tion must be stated to access the 3 rd mark

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
2	Ans: 8	
	• valid strategy	• knows to use $\pi r^2 h$
	• processing	• $\pi \times 3^2 \times 8 (= 226.19)$
	• processing a division	• $\frac{2000}{72\pi} (= 8.84)$
	• solution	• 8 (rounding down) 4RE
NOTES:		
(i)	the second mark is available only for a calcu	lation involving π and h
(ii)	the 3 rd mark is available for	
	either: explicit evidence of division of 2	000
	or: implicit evidence (unrounded con	nsistent value)
(iii)	the final mark is available for an answer consistent with the division (unrounded answer need not be stated)	
(iv)	if no rounding is required, the final mark cannot be awarded	

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
3	Ans: - 1.2, 5.2	
	• method	• substitution into quadratic formula
	• processing	• $\sqrt{40}$
	• solution	• -1.162, 5.162
	• rounding	• - 1.2, 5.2 4KU
NOTES:		
altern	ative evidence for 3 rd and 4 th marks	
(i)	3 rd mark (one solution and rounding) 4 th mark (another solution and rounding)	$\begin{array}{ccc} -1.162 \rightarrow & -1.2\\ 5.162 \rightarrow & 5.2 \end{array}$
(ii)	only the first mark is available for candidates	who process to a negative discriminant

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
4	Ans: 112.5 cm ²	
	linear scale factor	• $\frac{10}{4}$ or $\frac{4}{10}$
	• area scale factor	• $\left(\frac{5}{2}\right)^2$ or $\left(\frac{2}{5}\right)^2$
	• solution	• 112.5 3KU
NOTES:		
(i)	for 112.5 with or without working	award 3/3
(ii)	for 45 with or without working	award 1/3

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
5	Ans: £372, £74	
	• mean	• 372
	• standard deviation	• 74 2RE
NOTES:		

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
6 (a)	Ans: $y = 2x + 3$	
	• gradient	• 2
	• y-intercept	• (<i>c</i> =)3
	• gradient or intercept in equation	• $y = 2x \cdots$ or $y = \cdots + 3$
	• linear equation	• $y = 2x + 3$
		4KU
Notes:		
(i)	for a correct equation without working	award 4/4
(ii)	where the gradient and/or y-intercept are wro marks are still available	ong, but explicitly stated, the 3^{rd} and 4^{th}
(b)	Ans: 43	
	substitution	• 2×20+3
	• evaluation	• 43 2RE
Notes:		
(i)	for 43 with or without working	award 2/2

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
7 (a)	Ans: $t = \frac{k}{d^2}$ • statement of variation • formula	• $t \propto \frac{1}{d^2}$ • $t = \frac{k}{d^2}$
		2KU
(i) (ii)	evidence for the 2 nd mark may appear in p for any wrong variation, the 2 nd mark may	art (b) still be available
(b)	Ans: 8°C	
	• substitution	• $50 = \frac{k}{2^2}$
	• evaluating <i>k</i>	• <i>k</i> = 200
	• processing	• 8
		3KU
(i)	a maximum of $\frac{2}{3}$ is available for (a) (b)	direct variation $t \propto \frac{1}{d}$

Question No	Give 1 mark for each •	Illustrations of evid each n	ence for awarding nark
8	Ans: no, plus justification		
	• multiplying factor	• 0.8	r 20%
	• power of 3	• 0.8 ³	3 years
	• process	• 0.512	46.08
	communication	• no, because 51.2% > 50%	no, because 46.08 > 45
			4RE
NOTES:		ľ	
(i)	for 'simple' depreciation, only the final mark	is available	

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
9 (a)	 Ans: 20° solution 	• 20° 1KU
NOTES:		
(b)	 Ans: 55.6 m strategy substitution/processing solution 	 use of sine rule cosine rule median and right angled triangle correct application of valid strategy 55.6 3 RE
NOTES: (i) (ii)	accept solutions in radians or gradians for any attempt involving right angled trigon	ometry in $\triangle ABC$ award 0/3
(c)	 Ans: 312° strategy process 	 one of 180° + 80° 180° + 52° 52° + 80° 312°
NOTES:		2RE

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
10	Ans: 10 years	
	• substitution	• 83 = ···
	• process	• $M^2 - 4M - 60 = 0$
	• factorisation	• $(M-10)(M+6)=0$
	• solution	• 10 4RE
NOTES:		
(i)	if -6 is included in the final solution, the 4^{th}	mark cannot be awarded
(ii)	for an answer of 10 without working	award 1/4

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark	
11(a)	Ans: 2042 cm^2		
	• strategy	• $\frac{260}{360}$	
	• processing	$\bullet \frac{260}{360} \times \pi \times 30^2$	
	• solution	• 2042	
		3KU	
(i)	(i) $\frac{100}{360}$ can be awarded the 1 st mark only within the strategy $\pi r^2 - \frac{100}{360}\pi r^2$		
(b)	Ans: 136.1 cm		
	• strategy	• circumference of base = length of arc	
	• process	• $C = \frac{260}{360} \times \pi \times 60$	
	• process	• 136.1 3RE	
Notes: (i) o	calculating only $C = \pi \times 60$	award 0/3	

Question No	Give 1 mark for each •	Illustrations of evidence for awarding each mark
12 (a)	Ans: 210 • value	• 210 1KU
NOTES:		
(b)	Ans: proof	
	proof	• $\frac{1}{2}(n+1)(n+2)$ • $\frac{1}{2}(n^2+3n+2)$
Notes:	F	2 (* 2 * 2 * 2 * 2 * 2 * 2 * 2 * 2 * 2 *
(i)	for verifying formula for specific values	award 0/2
(c)	Ans: proof strategy 	• $\frac{1}{2}n(n+1) + \frac{1}{2}(n^2 + 3n + 2)$
	 factorising 	• $(n+1)(n+1)$ 2RE
Notes: (i)	for verifying formulae for specific values	award 0/2

KU 24 marks RE 28 marks

[END OF PAPER 2 MARKING INSTRUCTIONS]

Final KU 45 Totals RE 45