

# **2013 Mathematics**

# **Standard Grade – Credit**

# **Finalised Marking Instructions**

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### Part One: General Marking Principles for Mathematics Standard Grade - Credit

This information is provided to help you understand the general principles you must apply when marking candidate responses to questions in this Paper. These principles must be read in conjunction with the specific Marking Instructions for each question.

- (a) Marks for each candidate response must <u>always</u> be assigned in line with these general marking principles and the specific Marking Instructions for the relevant question. If a specific candidate response does not seem to be covered by either the principles or detailed Marking Instructions, and you are uncertain how to assess it, you must seek guidance from your Team Leader. For technical assistance, e-mail or phone the e-marker helpline.
- (b) Marking should always be positive ie, marks should be awarded for what is correct and not deducted for errors or omissions.

### **GENERAL MARKING ADVICE: Mathematics Standard Grade – Credit**

The marking schemes are written to assist in determining the "minimal acceptable answer" rather than listing every possible correct and incorrect answer. The following notes are offered to support Markers in making judgements on candidates' evidence.

#### **Special Instructions**

- 1 The main principle in marking scripts is to give credit for the skills which have been demonstrated. Failure to have the correct method may not preclude a pupil gaining credit for the calculations involved or for the communication of the answer.
- 2 The answer to one part, correct **or incorrect** must be accepted as a basis for subsequent dependent parts of a question. Full marks in the dependent part are possible if it is of equivalent difficulty.
- **3** Do not penalise insignificant errors. An insignificant error is one which is significantly below the level of attainment being assessed.
  - eg An error in the calculation of 16 + 15 would not be penalised at Credit Level.
- 4 Working after a correct answer should **only** be taken into account if it provides **firm** evidence that the requirements of the question have not been met.
- 5 In certain cases an error will ease subsequent working. **Full** credit cannot be given for this subsequent work but **partial** credit may be given.
- 6 Accept answers arrived at by inspection or mentally, where it is possible for the answer to have been so obtained.
- 7 Do not penalise omission or misuse of units unless marks have been specifically allocated to units.

8 A wrong answer without working receives no credit unless specifically mentioned in the marking scheme.

The rubric on the outside of the Papers emphasises that working must be shown. In general markers will only be able to give credit to partial answers if working is shown. However there may be a few questions where partially correct answers unsupported by working can still be given some credit. **Any such instances will be stated in the marking scheme.** 

**9** Acceptable alternative methods of solution can only be given the marks specified, ie a more sophisticated method cannot be given more marks.

Note that for some questions a method will be specified.

- 10 In general do not penalise the same error twice in the one question.
- 11 Accept legitimate variations in numerical/algebraic questions.
- 12 Do not penalise bad form eg sin  $x^{\circ} = 0.5 = 30^{\circ}$ .
- **13** A transcription error, where a number has been erroneously transcribed from the examination question, is not normally penalised except where the question has been simplified as a result.
- 14 When multiple solutions are presented by the candidate and it is not clear which is intended to be the final one, mark all attempts and award the lowest mark.
- 15 If a response has been scored out and not replaced, the response should be marked as normal.
- 16 If multiple responses have been scored out and not replaced, Note 14 applies.

### Part Two: Mathematics Standard Grade - Credit

# Paper 1

## Award marks in whole numbers only

Que	stion	Marking Scheme		Illustrations of evidence for awarding a
		Give 1 mark for each •	Mark	mark at each •
1		Evaluate		
		$86.5 - 3.651 \times 20$		
		Ans: 13·48	2	
		• <sup>1</sup> knowing correct order of operations		• <sup>1</sup> must involve a multiplication followed by a subtraction
		• <sup>2</sup> carrying out both calculations	(KU)	• <sup>2</sup> 13.48
Note	es:	· · · · · · · · · · · · · · · · · · ·		
(i)	for 13	3.48 with/without working		award 2/2
(ii)	ii) for 1656.98 with/without working			award 1/2
(iii)	for 73	3.02 with no further calculation		award 0/2

Que	stio	n	Marking Scheme	Max	Illustrations of evidence for awarding a	
-			Give 1 mark for each •	Mark	mark at each •	
2			Evaluate			
			$\frac{1}{2} \div 2\frac{2}{3}$			
			Ans: $\frac{3}{16}$	2		
			• <sup>1</sup> process		$\bullet^1$ $\frac{1}{2} \times \frac{3}{8}$	
			$\bullet^2$ a correct calculation	(KU)	$\bullet^2$ $\frac{3}{16}$	
Note	es:					
(i)	3				award 2/2	
(ii)	i) for $\frac{8}{6}$ or $1\frac{2}{6}$ with/without working award 1/2					
(iii)	3 1					

Question	Marking Scheme Give 1 mark for each •			Max	Illustrations of evidence for awarding a mark at each •	
				Mark		
3	help the The foll	o of people attended of stop smoking. owing table shows and after the course.				
		Mean number of cigarettes smoked per person per day	Standard deviation			
	Before	20.8	8.5			
	After	9.6	12.0			
	results.	wo valid comments ee below	about these	2		
	• <sup>1</sup> c	omment about mea	n		•1	on average fewer cigarettes were smoked per person after the course
		omment about stan eviation	dard		•2	the number of cigarettes smoked per person was more varied after the course
				( <b>RE</b> )		
Notes:						
(i) do no	ot accept '	the average number	of cigarettes	smoked n	er ner	'son was less'
(I) UO II	st accept	ine average number	or enguiettes	smoked p	er per	5011 1145 1055
(ii) do no	ot accept '	the standard deviati	on after the co	ourse was	greate	er'
(11) 00 110	st accept 1			Juise was	Sican	

Oue	stion	Marking Scheme	Max	Illustrations of evidence for awarding a	
		Give 1 mark for each •	Mark	mark at each •	
4		Change the subject of the formula to <i>r</i> . $A = 4\pi r^2$			
		Ans: $r = \sqrt{\frac{A}{4\pi}}$	2		
		• <sup>1</sup> starting process		• <sup>1</sup> $r^2 = \frac{A}{4\pi}$	
		• <sup>2</sup> finding the square root	(KU)	• <sup>2</sup> $r = \sqrt{\frac{A}{4\pi}}$	
Note	es:	·			
(i)	$r = \frac{\sqrt{A}}{\sqrt{4\pi}}$ award 2/2				
(ii)	for r	$=\frac{\sqrt{A}}{4\pi} \text{ or } \sqrt{\frac{A \div 4}{\pi}} \text{ or } \sqrt{A \div 4 \div \pi}$		award 1/2	
(iii)	i) the final mark is for taking the square root of the given $r^2$				

Question		Marking Scheme	Max	Illustrations of evidence for awarding a	
		Give 1 mark for each •	Mark	mark at each •	
5		<ul><li>150 patients have been given a flu vaccine.</li><li>The data is shown in the table below.</li></ul>			
		AGEGENDER $5 \text{ or under}$ 4 $5 \text{ or under}$ 4 $6-15$ 7 $16-59$ 37 $47$ $60 \text{ or over}$ 12 $32$ What is the probability that			
	a	a patient given the flu vaccine was male and aged 60 or over? Ans: $\frac{12}{150}$ or equivalent	1	1 12	
		• <sup>1</sup> process	(KU)	•1 $\frac{12}{150}$	
Not	es:				
(i)	Do	o not accept answer in ratio form	Γ		
5	b	a patient given the flu vaccine was aged 5 or under?			
		Ans: $\frac{7}{150}$	1		
		• <sup>1</sup> process	(KU)	• <sup>1</sup> $\frac{7}{150}$	
Not	es:		/	•	
(i)	an	answer in ratio form in part (b) may be award	led the ma	ark as a follow through error from (a)	

Que	estion	Marking Scheme	Max	Illustrations of evidence for awarding a
		Give 1 mark for each •	Mark	mark at each •
6		Joan buys gold and silver charms to make bracelets. 2 gold charms and 5 silver charms cost £125.		
	a	Let <i>g</i> pounds be the cost of one gold charm and <i>s</i> pounds be the cost of one silver charm.		
		Write down an equation in terms of $g$ and $s$ to illustrate the above information.		
		Ans: $2g + 5s = 125$	1	
		• <sup>1</sup> process	(KU)	$\bullet^1  2g + 5s = 125$
6		4 gold charms and 3 silver charms cost $\pm 145$ .		
	b	Write down another equation in terms of $g$ and $s$ to illustrate this information.		
		Ans: $4g + 3s = 145$	1	
		• <sup>1</sup> process	(KU)	$\bullet^1 \qquad 4g + 3s = 145$
6	с	Hence calculate the cost of each type of charm.		
		Ans: $g = 25; s = 15$	3	
		• <sup>1</sup> starting process		• <sup>1</sup> evidence of scaling
		• <sup>2</sup> value of one variable		• <sup>2</sup> $g = 25$
		• <sup>3</sup> value of a second variable	(RE)	• <sup>3</sup> $s = 15$
Not	es:		/	·
(i)	for g	g = 25 and $s = 15$ without working <b>but</b> check	ed in <b>bot</b>	<b>h</b> equations award $1/3$
(ii)	for g	g = 25 and $s = 15$ without working		award 0/3

Que	estion	Marking Scheme Give 1 mark for each •	Max Mark	Illustrations of evidence for awarding a mark at each •	
7	a	Expand and simplify $(2x-5)(x^2+3x-7)$ Ans: $2x^3 + x^2 - 29x + 35$			
		Ans: $2x + x - 29x + 35$ •1starting to expand•2continuing to process•3collecting like terms	3 (KU)	• <sup>1</sup> any 3 correct terms • <sup>2</sup> a further 3 correct terms • <sup>3</sup> $2x^3 + x^2 - 29x + 35$	
7	b	Solve the inequality $4x-5 \le 7x-20$ Ans: $x \ge 5$ or $5 \le x$ $\bullet^1$ dealing with variable $\bullet^2$ dealing with constant $\bullet^3$ solution	3 (KU)	• <sup>1</sup> -3x or 3x • <sup>2</sup> -15 or 15 • <sup>3</sup> $x \ge 5$ or $5 \le x$	

Question	Marking Scheme	Max	Illustrations of evidence for awarding a	
	Give 1 mark for each •	Mark	mark at each •	
8	Four straight line graphs are shown below.			
	$\begin{array}{c c} A & y & & & & \\ \hline & y & & & & \\ \hline & & & & & \\ \hline & & & & & \\ \hline & & & &$			
	$\begin{array}{c c} C & y & D & y \\ \hline & & & \\ \hline & & \\ \hline & & & \\ \hline \\ \hline$			
	Which one of these above could represent the line with equation 2x + y = 3?			
	Give two reasons to justify your answer.			
	Ans: graph D	3		
	• <sup>1</sup> re-arranging		• <sup>1</sup> $y = -2x + 3$	
	• <sup>2</sup> understanding		• <sup>2</sup> $m$ – negative $c$ – positive	
	$\bullet^3$ conclusion	(RE)	$\bullet^3$ D	
Notes:				
i) for a	n answer with no working		award 0/3	
	andidates who do not re-arrange, the 1 <sup>st</sup> m cept are stated	ark can be	e awarded only if the correct gradient and	

Question		n Marking Scheme	Max	Illustrations of evidence for awarding a				
~		Give 1 mark for each •	Mark	mark at each •				
9	a	<ul> <li>Quick-Smile photographers charge the following rates:</li> <li>50p per photograph for the first 12 photographs printed</li> <li>35p per photograph for any further photographs printed</li> <li>£4.25 for a CD of the photographs.</li> <li>How much will it cost to have 16 photographs printed plus a CD?</li> </ul>						
		<ul> <li>Ans: £11.65</li> <li>•<sup>1</sup> starting the process</li> </ul>	2	• <sup>1</sup> either $(12 \times 0.5)+4.25$ or $(16-12) \times 0.35$				
		$\bullet^2$ calculation	(KU)	$\bullet^2$ £11.65				
(ii)	th	e 2 <sup>nd</sup> mark may be awarded <b>only</b> for a correc	t calculatio	on involving all 3 rates.				
9	b	Find a formula for C, the cost in pounds, of having <i>x</i> photographs printed (where <i>x</i> is greater than 12) plus a CD.						
		Ans: $(c =) 6 + (x-12) 0.35 + 4.25$	3					
		• <sup>1</sup> starting strategy		• <sup>1</sup> $12 \times 0.5$				
		$\bullet^2$ continuing strategy		• <sup>2</sup> $(x-12) \times 0.35$				
		• <sup>3</sup> formula	(RE)	• <sup>3</sup> $6 + (x - 12) \cdot 0 \cdot 35 + 4 \cdot 25$				
		1	()	1				
Not	es:							
Not		nore subsequent simplification						

Que	Question		Marking Scheme		Illustrations of evidence for awarding a	
		1	Give 1 mark for each •	Mark	mark at each •	
10			The parabola with equation $y = x^2 - 2x - 3$ cuts the <i>x</i> -axis at the points A and B as shown in the diagram. $y = x^2 - 2x - 3$ A = B = x			
	a		Find the coordinates of A and B.			
			Ans: A(-1,0), B(3,0)	4		
			• <sup>1</sup> equating to zero		$\bullet^1 \qquad x^2 - 2x - 3 = 0$	
			• <sup>2</sup> factorising		• <sup>2</sup> $(x-3)(x+1) = 0$	
			• <sup>3</sup> solving for $x$		• <sup>3</sup> $x = -1$ or 3	
			• <sup>4</sup> co-ordinates	(RE)	• <sup>4</sup> A(-1,0), B(3,0)	
Not	es:					
(i)	ec	quati	ing to zero must appear prior to solving for	r x		
(ii)	fc	or co	rrect coordinates with no working	av	ward 0/4	
			-			
(iii)	Ca	andi	dates may draw graph – check page 15 on	answer bo	ooklet	
10	b		Write down the equation of the axis of symmetry of $y = x^2 - 2x - 3$ .			
			<b>Ans:</b> $x = 1$	1		
			• <sup>1</sup> calculation	(KU)	• <sup>1</sup> $x = 1$	
Not	es:			(110)	1	
			awar of 1 is not sufficient to said the work	r		
(i)	al	i ans	swer of 1 is not sufficient to gain the mar	ĸ		

Qu	estion	Marking Scheme	Max	Illustrations of evidence for awarding a
	1 1	Give 1 mark for each •	Mark	mark at each •
11		Jenny is doing calculations using consecutive numbers.		
		She notices a pattern which always gives an answer of 1.		
		Using 2, 3, 4 gives $3^2 - 2 \times 4 = 1$ . 3, 4, 5 gives $4^2 - 3 \times 5 = 1$ . 4, 5, 6 gives $5^2 - 4 \times 6 = 1$ .		
	a	Using 8, 9, 10, write down a similar pattern.		
		<b>Ans:</b> $9^2 - 8 \times 10 = 1$	1	
		• <sup>1</sup> statement	(KU)	$\bullet^1 \qquad 9^2 - 8 \times 10 = 1$
Not	es:			
(i)	do n	tot accept $9^2 - 8 \times 10$		
11	b	Using n, $(n + 1)$ , $(n + 2)$ , show that the answer is 1 for any three consecutive numbers.		
		Ans: proof	3	
		• <sup>1</sup> beginning proof		• <sup>1</sup> $(n+1)^2 - n (n+2)$ • <sup>2</sup> $n^2 + 2n + 1 - n^2 - 2n$
		$\bullet^2$ simplification		$\bullet^2 \qquad n^2 + 2n + 1 - n^2 - 2n$
		• <sup>3</sup> proof	(RE)	• <sup>3</sup> 1
Not	tes:			1
(i)	for t	he 2 <sup>nd</sup> mark, brackets must be explicitly ex	panded	
			-	
(ii)	the 3	3 <sup>rd</sup> mark can be awarded only if the 2 <sup>nd</sup> mar	k has bee	n awarded

KU 20 RE 18

### [END OF PAPER 1 MARKING INSTRUCTIONS]

## Paper 2

# Award marks in whole numbers only

Ques	stion	Marking Scheme Give 1 mark for each •	Max Mark	Illustrations of evidence for awarding a mark at each •
1		A snail crawls 3 kilometres in 16 days.		
		What is the average speed of the snail in metres per second?		
		Give your answer <b>in scientific</b> <b>notation correct to 2 significant</b> <b>figures</b> .		
		<b>Ans:</b> $2 \cdot 2 \times 10^{-3}$	4	
		• <sup>1</sup> evidence of correct formula with units		• <sup>1</sup> $\frac{3km}{16 \text{ days}}$
		• <sup>2</sup> correct conversion of units		$\bullet^2 \qquad \frac{3000}{16 \times 24 \times 60 \times 60}$
		• <sup>3</sup> unrounded solution		• <sup>3</sup> 0.00217
		• <sup>4</sup> correct rounding and scientific notation		• <sup>4</sup> $2 \cdot 2 \times 10^{-3}$
Note	s:		(KU)	
(i)	for 2.	$2 \times 10^{-3}$ with/without working		award 4/4
(ii)	for 2.	$17 \dots \times 10^{-3}$ , with or without working		award 3/4
(iii)	for $\frac{3}{1}$	$\frac{3}{6}$ , leading to $1.9 \times 10^{-1}$		award 1/4
(iv)	for $\frac{3}{1}$	$\frac{3}{6}$ , followed by $\frac{3000}{16 \times 24 \times 60 \times 60}$		award the first two marks
(v)	for $\frac{3}{1}$	$\frac{3}{6}$ , followed by a correct partial conversion	on	award the first mark

Que	stion	Marking Scheme		Max	Illustrations of evidence for awarding a		
-			Give 1 mark for each •		mark at each •		
2		$2x^2 + \frac{1}{2}$ Give y	the equation 7x - 3 = 0 your answers <b>correct to 1</b> <b>nal place</b> .				
			0.4 or -3.9	4			
		• <sup>1</sup>	correct substitution into quadratic formula		$\bullet^1 \qquad \frac{-7 \pm \sqrt{7^2 - 4 \times 2 \times -3}}{4}$		
		• <sup>2</sup>	correct discriminant		• <sup>2</sup> 73		
		• <sup>3</sup>	unrounded solution		• <sup>3</sup> 0.385, $-3.885$		
		• <sup>4</sup>	rounded solution	(KU)	• <sup>4</sup> 0·4, -3·9		
Note	es:			(110)			
	alte	ernative	e evidence for 3 <sup>rd</sup> and 4 <sup>th</sup> marks				
	3 <sup>rd</sup> 1	mark (o	ne solution and rounded)	0.385	$\rightarrow 0.4$		
	4 <sup>th</sup> 1	mark (a	nother solution and rounded)	- 3.88	$35 \rightarrow 3.9$		
(i)	only	only the first mark is available for candidates who process to a negative discriminant					
(ii)	unles	SS	ho do not give an unrounded num wer is $0.4$ , $-3.9$ where $3/4$ may be		t be awarded the last 2 marks,		

Que	estion	n Marking Scheme	Max	Illustrations of evidence for awarding a
		Give 1 mark for each •	Mark	mark at each •
3	а	A concrete block is in the shape of a prism. $\begin{array}{c} 22cm \\ 22cm \\ 32cm \\ \hline 32cm \\ \hline \\ \hline$		
		<b>Ans:</b> 540 cm <sup>2</sup>	2	
		Ans: 540 cm	3	
		• <sup>1</sup> beginning process		• <sup>1</sup> $2 \times \frac{1}{2} \times 5 \times 20 + (22 \times 20)$ or
				$\frac{1}{2} \times 20 \times (22 + 32)$
		• <sup>2</sup> processing		• <sup>2</sup> 100 + 440 or $10 \times 54$
		$\bullet^3$ calculation	(KU)	• <sup>3</sup> 540
3	b	Calculate the volume of the concrete block.		
		Ans: 32 400 cm <sup>3</sup>	1	
		$\bullet^1$ calculation	(KU)	• <sup>1</sup> 32 400

Que	stion		ng Scheme	Max	Illustrations of evidence for awarding a mark at each •			
		Give 1	mark for each •	Mark				
4		"Topfl	ear, 1296 learner drivers from ight" school of motoring passed riving test.					
			as 72% of those who sat their g test from Topflight.					
		How n	nany failed their driving test?					
		Ans:	504	3				
		• <sup>1</sup>	valid strategy		• <sup>1</sup>	72% = 1296		
		•2	processing		•2	$1\% = \frac{1296}{72} = 18$		
		• <sup>3</sup>	solution	(RE)	•3	$18 \times 28 = 504$		
Note	s:							
(i)	for 504, with/without working award 3/3							
(ii)	i) for candidates who calculate either 28% or 72% of 1296 award 0/3							
(iii)	the fi	nal mark	t is for multiplying 1% by 28					

Que	stion	Marking Scheme	Max	Illustrations of evidence for awarding a	
		Give 1 mark for each •	Mark	mark at each •	
5		ABC is an isosceles triangle with angle ACB = $30^{\circ}$ .	è		
		AC = BC = x centimetres.			
		C x  cm $30^{\circ}$ $x \text{ cm}$ A $BThe area of triangle ABC is 9 squarecentimetres. Calculate the value of x.$			
		Ans: $x = 6$	3		
		• <sup>1</sup> correct substitution into area formula		• <sup>1</sup> $9 = \frac{1}{2} \times x^2 \times \sin 30^\circ$	
		• <sup>2</sup> processing		• <sup>2</sup> 36	
		• <sup>3</sup> solution	(RE)	• <sup>3</sup> $x = 6$	
Note	s:	1	(112)	1	
(i)	accep	of $9 = \frac{1}{2}$ ab sin 30° for first mark			

Ques	stion		ing Scheme	Max		rations of evidence for awarding a
		Give 1	l mark for each •	Mark	mark	at each •
6		high, s a circl It is su metres a poin	bile phone mast, 18.2 metres stands vertically in the centre of e. apported by a wire rope, 19 s long, attached to the ground at t on the circumference of the as shown.			
			19 m 18·2 m			
		Calcul circle.	ate the circumference of the			
		Ans:	34·3 m	3		
		$\bullet^1$	correct use of Pythagoras		• <sup>1</sup>	$r^2 = 19^2 - 18 \cdot 2^2$
		• <sup>2</sup>	calculating radius		•2	5.455
		•3	calculating circumference	(KU)	•3	34.3

Question	Marking Scheme	Max	Illustrations of evidence for awarding a	
-	Give 1 mark for each •	Mark	mark at each •	
7	Jack weighs 94 kilograms. On the 1st of January, he starts a diet which is designed to reduce his weight by 7% per month. During which month should he achieve his target weight of 73 kilograms?			
	Show all your working. Ans: during April	4		
	• <sup>1</sup> reduction factor	-	• <sup>1</sup> 0.93	
	• <sup>2</sup> processing		$\bullet^2 \qquad 0.93 \times 94 = 87.42$	
	$\bullet^3$ continuation		• <sup>3</sup> 75·6	
	• <sup>4</sup> communication	(RE)	• <sup>4</sup> During April or 4 <sup>th</sup> month	
Notes:	1	()	1	

Question	Marking Scheme Give 1 mark for each •	Max Mark	Illustrations of evidence for awarding a mark at each •	
8	As the pendulum of a clock swings, its tip moves through an arc of a circle. 50  cm $B$ $36.7  cm$			
	The length of the pendulum is 50 centimetres. The length of the arc is $36.7$ centimetres. Calculate $x^{\circ}$ , the angle through which the pendulum swings.			
	<b>Ans: 42°</b>	3		
	• <sup>1</sup> strategy		$\bullet^1$ $\frac{x}{360}$	
	$\bullet^2$ strategy		$\bullet^2 \qquad \frac{36\cdot 7}{100\pi}$	
	$\bullet^3$ solution	(RE)	$\bullet^3$ 42°	
Notes:				
(i) for u	se of $C = \pi r^2$ , the 1 <sup>st</sup> and 3 <sup>rd</sup> marks are still	available		

Question		Max	Illustrations of evidence for awarding a mark at each •	
	Give 1 mark for each •	Mark		
9	In triangle THB: • angle TBH = $90^{\circ}$ • angle THB = $32^{\circ}$ G is a point on HB. • angle TGB = $57^{\circ}$ • GH = 46 metres.			
	$H \xrightarrow{32^{\circ}} 57^{\circ} B$			
	Calculate the length of TB.			
	Ans: 48·4 m	4		
	• <sup>1</sup> correct use of sine rule in triangle THG		• <sup>1</sup> $\frac{\mathrm{TG}}{\sin 32^{\circ}} = \frac{46}{\sin 25^{\circ}}$	
	$\bullet^2$ calculation		• <sup>2</sup> TG = $57.679$	
	• <sup>3</sup> appropriate trig ratio		• <sup>3</sup> $\sin 57^\circ = \frac{TB}{57 \cdot 679}$	
	• <sup>4</sup> solution	(KU)	• <sup>4</sup> TB = $48 \cdot 37 \dots$	
Notes:		/	1	
Notes:				

(ii) the  $2^{nd}$  and  $4^{th}$  marks are available only within a valid strategy

Que	estio	n	Marking Scheme	Max	Illustrations of evidence for awarding a
			Give 1 mark for each •	Mark	mark at each •
10			A function is given by the formula, $f(x) = 4 \times 2^x$ .		
	a		Evaluate $f(3)$ .		
			Ans: 32	2	
			• <sup>1</sup> substitution		• <sup>1</sup> $4 \times 2^3$
			$\bullet^2$ calculation	(KU)	• <sup>2</sup> 32
10	b		Given that $f(m) = 4$ , find the value of $m$ .		
			Ans: $m = 0$	2	
			• <sup>1</sup> substitution		• <sup>1</sup> $4 = 4 \times 2^m$
			• <sup>2</sup> solution	(RE)	• <sup>2</sup> $m=0$

Question		n Marking Scheme	Max	Illustrations of evidence for awarding a	
		Give 1 mark for each •	Mark	mark at each •	
11		Water flows through a horizontal pipe of diameter 60 centimetres. The surface width, AB, of the water is 55 centimetres.			
		$d \downarrow^{A}$ $B \downarrow^{60 \text{ cm}}$			
	a	Calculate the depth, <i>d</i> , of the water in the pipe.			
		Ans: 18.01 cm	4		
		• <sup>1</sup> recognition of right angle		• <sup>1</sup> use of Pythagoras	
		• <sup>2</sup> processing		• <sup>2</sup> $30^2 - 27 \cdot 5^2$	
		• <sup>3</sup> processing		• <sup>3</sup> 11.99	
		$\bullet^4$ solution	(KU)	• <sup>4</sup> 18·01	
Not	es:				
(i)	fo	one mark, the right angle may be stated or	indicated of	on a diagram	
11	b	What other depth of water would give the same surface width?			
		Ans: 41.99 cm	1		
		• <sup>1</sup> communication		• <sup>1</sup> 41.99	
			(RE)		

Ques	stion			Max	Illustrations of evidence for awarding a	
		Give 1 mark for each •	Mark	mark at each •		
12			of the graph of $y = 1 + \sin x^{\circ}$ is n in the diagram below. $y = 1 + \sin x^{\circ}$ A B $y = 1 \cdot 7$ x			
			ine $y = 1.7$ is drawn. It cuts the of $y = 1 + \sin x^{\circ}$ at A and B as n.			
		Calcu B.	late the <i>x</i> -coordinates of A and			
		Ans:	44·4°, 135·6°	4		
		• <sup>1</sup>	equating functions		• <sup>1</sup>	$1 + \sin x^{o} = 1 \cdot 7$
		• <sup>2</sup>	processing		• <sup>2</sup>	$\sin x^{\mathbf{o}} = 0.7$
		• <sup>3</sup>	first solution		• <sup>3</sup>	44·4°
		• <sup>4</sup>	second solution	(RE)	• <sup>4</sup>	135·6 <sup>°</sup>
Note	s:	1		()	1	
(i)			who obtain a negative value of sin x the 3rd and 4th quadrants	t may still	be aw	arded the last two marks
(ii)	candi	dates w	who give more than two answers <b>ca</b>	nnot be a	warde	d the last mark
(iii)	cauti		$44 \cdot 4^{\circ} + 90^{\circ} = 134 \cdot 4^{\circ}$ this is close to the correct answer			

Question	Marking Scheme	Max Mork	Illustrations of evidence for awarding a	
	Give 1 mark for each •	Mark	mark at each •	
13	Asim has a poster which is 25 centimetres wide and 40 centimetres high.			
	40 cm			
	He decides to place it on a white card. The card and the poster are mathematically similar.			
	The border is 5 centimetres wide on three sides and $x$ centimetres wide on the fourth side as shown.			
	5 cm 5 cm x cm			
	Calculate the value of <i>x</i> .			

Question	Marking Scheme	Max	Illustrations of evidence for awarding a
	Give 1 mark for each •	Mark	mark at each •
13	<b>Ans:</b> $x = 11$	4	
	Method 1		25
	• <sup>1</sup> strategy		• <sup>1</sup> scale factor = $\frac{35}{25}$
	$\bullet^2$ applying scale factor		• <sup>2</sup> $\left(\frac{7}{5}\right) \times 40$
	• <sup>3</sup> processing		• <sup>3</sup> 56
	$\bullet^4$ solution		• <sup>4</sup> 11
	Ans: $x = 11$		
	Method 2		
	• <sup>1</sup> strategy		• $\frac{25}{40}$ or $\frac{35}{45+x}$
	$\bullet^2$ equating ratios		• <sup>2</sup> $\frac{25}{40} = \frac{35}{45+x}$
	$\bullet^3$ cross multiplication		• <sup>3</sup> $25(45 + x) = 35 \times 40$
	$\bullet^4$ solution		• <sup>4</sup> 11
		(RE)	

Question	Marking Scheme Give 1 mark for each •	Max Mark	Illustrations of evidence for awarding a mark at each •
14	In triangle ABC: • $\cos A = 0.5$ • $AB = 6$ centimetres • $BC = 2x$ centimetres • $AC = x$ centimetres • $AC = x$ centimetres		
	B $2x \text{ cm}$ C Show that $x^2 + 2x - 12 = 0$		
	Ans: $x^2 + 2x - 12 = 0$	3	
	• <sup>1</sup> substitution into cosine rule		• <sup>1</sup> $(2x)^2 = x^2 + 6^2 - 2 \times x \times 6 \times 0.5$
	• <sup>2</sup> processing		• <sup>2</sup> $4x^2 = x^2 - 6x + 36$
	• <sup>3</sup> completion of proof	(RE)	• <sup>3</sup> $x^2 + 2x - 12 = 0$
Notes:			
(i) $2x^2$ is	s to be treated as bad form for the 1 <sup>st</sup> mark		
(ii) the fi	inal mark is given only for an explicit state	ement	

KU 25 RE 27

OVERALL TOTAL MARKS 45 KU 45 RE

## [END OF PAPER 2 MARKING INSTRUCTIONS]