

Sequences and Series 2

1. Given $f(x) = \frac{1}{(x-2)^4}$, $|x| < 1$,
obtain the Maclaurin expansion of $f(x)$ as far as the term in x^4 .
2. Write down Maclaurin expansion of $\cos x$ and hence find the first three non-zero term of the Maclaurin expansion for $f(x) = \cos 3x$.
3. Using the Maclaurin expansion of e^x , calculate $e^{0.2}$ correct to 3 decimal places.
4. Find the expansion of $f(x) = (1+2x)\ln(1+x)$ as far as the term in x^5 .
5. Given that $\frac{1}{1-x} = 1 + x + x^2 + x^3 + x^4 + \dots$, $|x| < 1$, find the first 5 terms in the expansion of $f(x) = \frac{3}{1+x-2x^2}$ and state the region of validity for x .
(Hint: use partial fractions)